Geometry H
8.3: Show that a Quadrilateral is a Parallelogram

Name: $\qquad$
Date: $\qquad$ Period: $\qquad$

- I can use properties to identify parallelograms.
- I can use coordinate geometry to identify parallelograms.

TARGETS

You can use the following conditions to determine whether a quadrilateral is a parallelogram.

## Conditions for Parallelograms

A quadrilateral is a parallelogram if....

- Both pairs of opposite sides are parallel (definition)
- Both pairs of opposite sides are congruent.
- Both pairs of opposite angles are congruent.
- The diagonals bisect each other.
- One pair of opposite sides is congruent and parallel.


## Example 1: Identify parallelograms

Explain how you know that quadrilateral $Q R S T$ is a parallelogram.
a)



Example 2: Solve a real world problem
The figure shows part of a stair railing. Explain how you know that the support bars $\overline{M P}$ and $\overline{Q N}$ are parallel.

Example 3: Use coordinate Geometry to identify parallelograms
a) The vertices of $A B C D$ are $A(-3,1), B(-1,0), C(4,5)$, and $D(2,6)$. Show that $A B C D$ is a parallelogram using the definition of parallelograms.

b) The vertices of $L M N O$ are $L(-4,2), M(-5,-2), N(-1,-4)$ and $O(0,0)$. Show that LMNO is a parallelogram using the diagonals.

c) Use the $L M N O$ from example b, prove that $L M N O$ is a parallelogram using sides $\overline{L M}$ and $\overline{N O}$ only.
d) Could we prove a quadrilateral is a parallelogram using only side lengths?

