Geometry H 8.3: Show that a Quadrilateral is a Parallelogram

Name: _	
Date: _	Period:



I can use properties to identify parallelograms.

• I can use coordinate geometry to identify parallelograms.

You can use the following conditions to determine whether a quadrilateral is a parallelogram.

Conditions for Parallelograms

A quadrilateral is a parallelogram if....

- Both pairs of opposite sides are parallel (definition)
- Both pairs of opposite sides are congruent.
- Both pairs of opposite angles are congruent.
- The diagonals bisect each other.
- One pair of opposite sides is congruent and parallel.

Example 1: Identify parallelograms

Explain how you know that quadrilateral QRST is a parallelogram.







Example 2: Solve a real world problem

The figure shows part of a stair railing. Explain how you know that the support bars \overline{MP} and QN are parallel.



Example 3: Use coordinate Geometry to identify parallelograms

a) The vertices of *ABCD* are A(-3, 1), B(-1,0), C(4, 5), and D(2, 6). Show that *ABCD* is a parallelogram using the definition of parallelograms.



b) The vertices of *LMNO* are *L*(-4, 2), *M*(-5, -2), *N*(-1, -4) and *O*(0, 0). Show that LMNO is a parallelogram using the diagonals.



c) Use the *LMNO* from example b, prove that *LMNO* is a parallelogram using sides \overline{LM} and \overline{NO} only.

d) Could we prove a quadrilateral is a parallelogram using only side lengths?