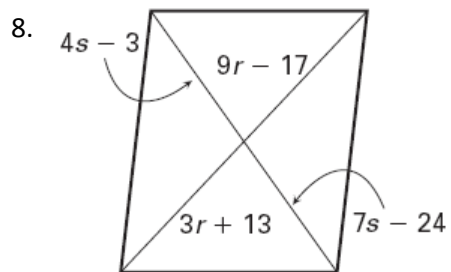
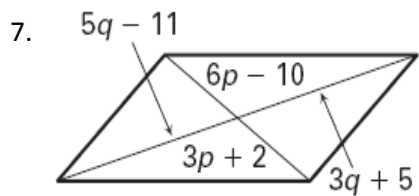
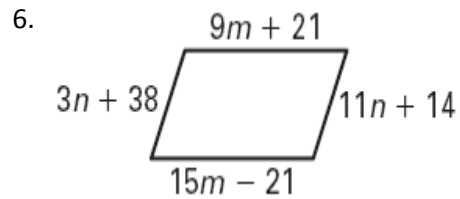
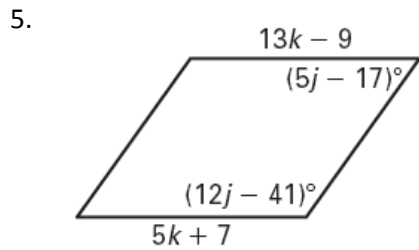
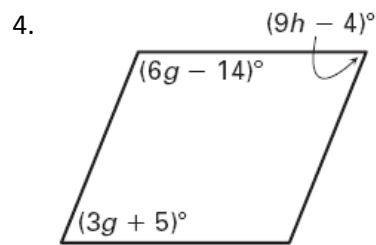
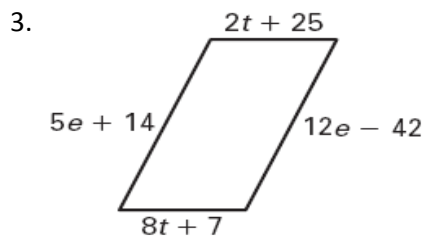
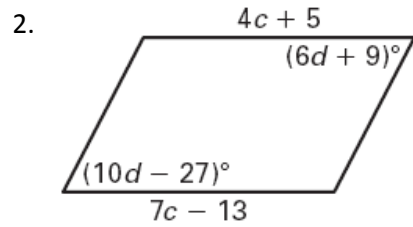
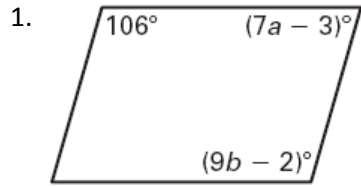
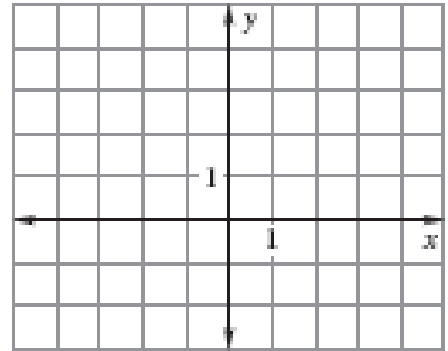


Find the value of each variable in the parallelogram.

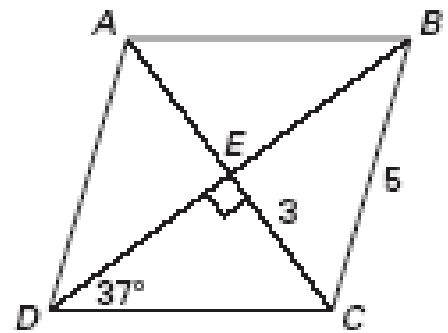


9. The coordinates for $\square ABCD$ are $A(-1, 3)$, $B(4, 2)$, $C(2, -1)$, and $D(-3, 0)$. Plot the points and draw $\square ABCD$ on the coordinate plane. Then draw the diagonals \overline{AC} and \overline{BD} . Label the intersection of the diagonals as point E . What are the coordinates of point E ?



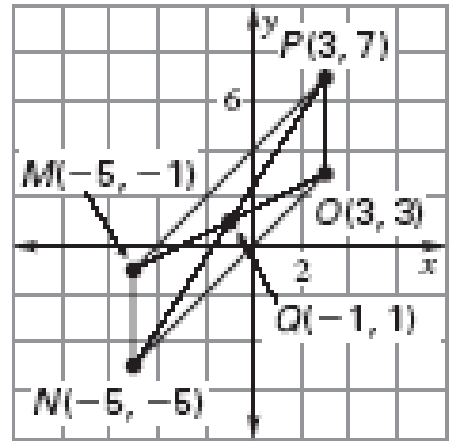
10. Find the indicated measure in $\square ABCD$. Explain.

- a. AE
- b. AD
- c. EB
- d. DB
- e. AB
- f. Perimeter of $\triangle AEB$
- g. $m\angle DBA$
- h. $m\angle DEC$
- i. $m\angle ACD$
- j. $m\angle CAB$
- k. Perimeter of $\square ABCD$



11. The measure of one interior angle of a parallelogram is 2.6 times the measure of another angle. Find the measure of each angle.
12. The measure of one interior angle of a parallelogram is 57.8 degrees more than the measure of another angle. Find the measure of each angle.

13. Use the diagram of $\square MNOP$ at the right.



a) Use the distance formula to show $\overline{MP} \cong \overline{NO}$

b) Use the distance formula to show $\overline{MN} \cong \overline{PO}$.

c) Find the slopes of \overline{MP} and \overline{NO} .

d) How do the slopes found in part c show that \overline{MN} and \overline{PO} are parallel?

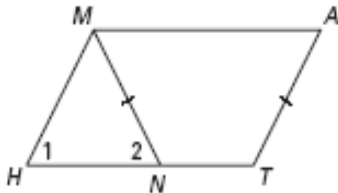
e) Use the midpoint formula to show that the diagonals bisect each other.

14. Complete the following proof.

GIVEN: $MATH$ is a \square .

$$\overline{MN} \cong \overline{AT}$$

PROVE: $\angle 1 \cong \angle 2$



Statements

Reasons

1. $MATH$ is a \square .

1. $\underline{\quad?}$

2. $\underline{\quad?}$

2. Given

3. $\overline{MH} \cong \overline{AT}$

3. $\underline{\quad?}$

4. $\underline{\quad?}$

4. Transitive Property of \cong

5. $\angle 1 \cong \angle 2$

5. $\underline{\quad?}$

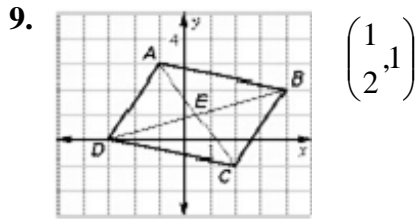
The given point coordinates represent three vertices of a parallelogram. Write the coordinates of each other point that could be the fourth vertex. *Justify* your answers.

15. A(2, 0), B(3, 5), C(6, 0)

16. J(a, b), K(a+2, b), L(a+4, b+3)

Answer Key

1. $a = 11, b = 12$
2. $c = 6, d = 9$
3. $e = 8, t = 3$
4. $g = 21, h = 8$
5. $j = 14, k = 2$
6. $m = 7, n = 3$
7. $p = 4, q = 8$
8. $r = 5, s = 7$



10. a) 3; Diagonals of \square bisect each other.
 b) 5; Opposite sides of \square are \cong .
 c) 4; Pythagorean Theorem
 d) 8; Diagonals of \square bisect each other, so $DB = 2EB$.
 e) 5; Pythagorean Theorem or SAS \cong Theorem
 f) 12; $P = 3+4+5=12$
 g) 37° ; Alternate Interior Angles Theorem
 h) 90° ; Definition of a right triangle
 i) 53° ; Triangle Sum Theorem
 j) 53° ; Alternate Interior Angles Theorem
 k) 20; All 4 Δ 's are \cong with hypotenuse = 5.
11. 50° and 130°
12. 61.1° and 118.9°
13. a) $MP = 8\sqrt{2}$ and $NO = 8\sqrt{2}$, so $\overline{MP} \cong \overline{NO}$
 b) $MN = 4$ and $PO = 4$, so $\overline{MN} \cong \overline{PO}$
 c) slope of $\overline{MP} = 1$, and slope of $\overline{NO} = 1$
 d) Parallel lines have the same slope.
 e) The midpoint of \overline{MO} is $(-1, 1)$ and midpoint of \overline{PN} is $(-1, 1)$. Since they intersect each other at their midpoint, they bisect each other.
14. Given; $\overline{MN} \cong \overline{AT}$; Opposite sides of \square are \cong ; $\overline{MN} \cong \overline{MH}$; Base Angles Theorem
15. $(-1, 5), (7, 5)$
16. $(a + 2, b + 3), (a + 6, b + 3)$