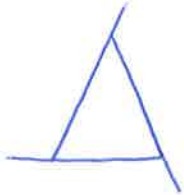


1. Is each of the following statements true or false? Explain your reasoning.

- a. Every equilateral triangle is acute. *True, each angle in an equilateral Δ is 60° .*
- b. A triangle can have two obtuse angles. *False, a triangle can have at most one obtuse angle*
- c. A triangle can have two acute exterior angles. *False, if a Δ is acute, all ext. angles will be obtuse
if a Δ is obtuse, only one ext angle will be acute*
- d. A triangle can have at most one right angle. *True*



2. In $\triangle DEF$, $m\angle D = (12x - 6)^\circ$, $m\angle E = (5x + 2)^\circ$, and $m\angle F = 6x^\circ$. Classify $\triangle DEF$ by its angles.

$$23x - 4 = 180$$

$$23x = 184$$

$$\boxed{x = 8}$$

$$m\angle D = 90^\circ$$

$$m\angle E = 42^\circ$$

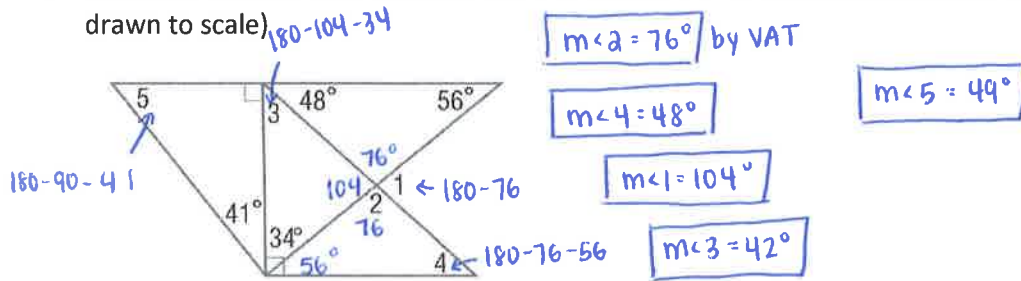
$$m\angle F = 48^\circ$$

> Right Δ

3. A triangle has side lengths of 4 inches, 6 inches, and 8 inches. Classify the triangle by its side lengths.

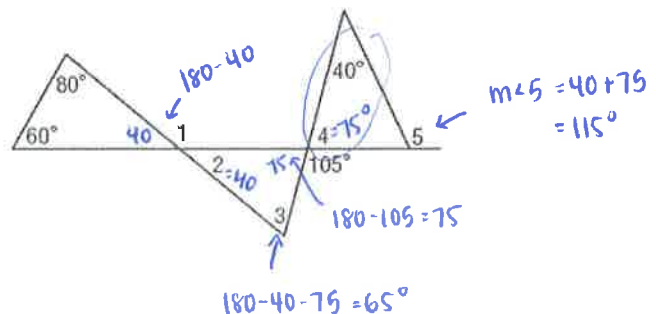
Scalene because all side lengths are different

4. Using the diagram below, please find the measure of all numbered angles. (NOTE: Diagram not drawn to scale)

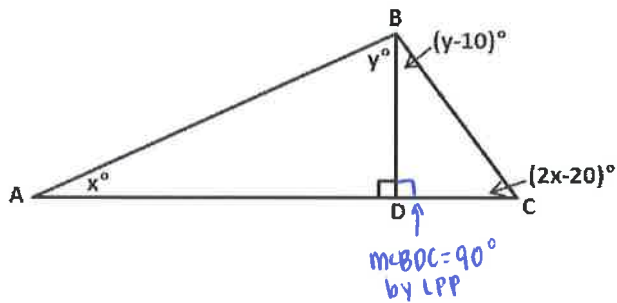


5. Using the diagram below, please find the measure of the following angles:

- a. $m\angle 1 = 140^\circ$
- b. $m\angle 2 = 40^\circ$ (by VAT)
- c. $m\angle 3 = 65^\circ$
- d. $m\angle 4 = 75^\circ$ (by VAT)
- e. $m\angle 5 = 115^\circ$



6. Using the diagram below, please solve for x and y.



$$\begin{aligned} \Delta ABD: \quad x + y + 90 &= 180 \\ x + y &= 90 \end{aligned}$$

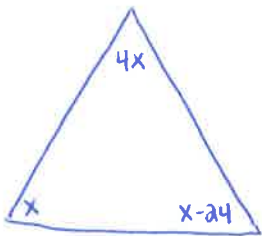
$$\begin{aligned} \Delta BDC: \quad y - 10 + 2x - 20 + 90 &= 180 \\ 2x + y + 60 &= 180 \\ 2x + y &= 120 \end{aligned}$$

$$\text{System: } \begin{cases} x + y = 90 \\ 2x + y = 120 \end{cases}$$

$$\Rightarrow \begin{aligned} -x - y &= -90 \\ 2x + y &= 120 \\ \hline x &= 30 \end{aligned}$$

$$\begin{aligned} 30 + y &= 90 \\ y &= 60 \end{aligned}$$

7. In a triangle, the measure of the second angle is four times the measure of the first angle. The third angle is twenty-four less than the first angle. Find the measure of each angle and classify the triangle by its angle measures **and** by its side lengths.



$$x + 4x + x - 24 = 180$$

$$6x - 24 = 180$$

$$6x = 204$$

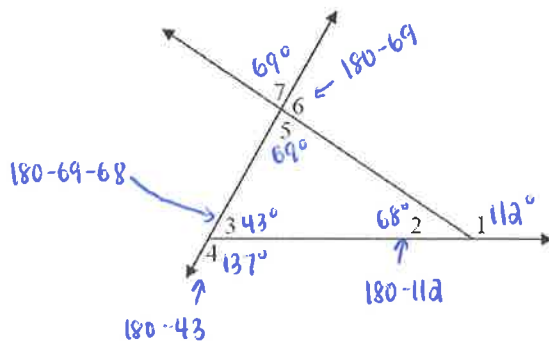
$$\boxed{x = 34}$$

$$\begin{aligned} \text{First angle} &= 34^\circ \\ \text{Second} &= 136^\circ \\ \text{Third} &= 10^\circ \end{aligned}$$

Obtuse scalene
↑
one angle greater than 90°

↑
all angles are different which means all sides are different

8. Given $m\angle 1 = 112^\circ$ and $m\angle 7 = 69^\circ$, find the measures of the other numbered angles.



$$m\angle 1 = 112^\circ$$

$$m\angle 2 = 68^\circ$$

$$m\angle 3 = 43^\circ$$

$$m\angle 4 = 137^\circ$$

$$m\angle 5 = 69^\circ$$

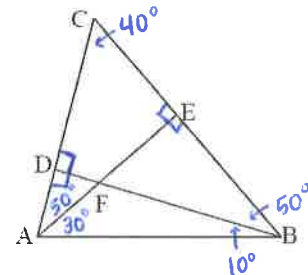
$$m\angle 6 = 111^\circ$$

$$m\angle 7 = 69^\circ$$

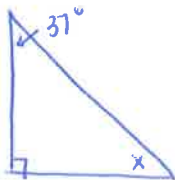
9. In the diagram below, $m\angle CAB = 80^\circ$ and $m\angle CBA = 60^\circ$. If $\overline{BD} \perp \overline{AC}$ and $\overline{AE} \perp \overline{BC}$, find $m\angle ACB$ and $m\angle AFB$.

$$m\angle ACB = 40^\circ$$

$$m\angle AFB = 140^\circ$$



10. One acute angle of a right triangle measures 37° . Find the measure of the other acute angle.



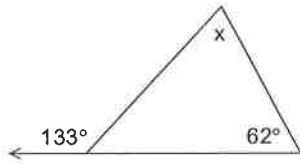
$$x + 37 = 90$$

$$x = 53^\circ$$

The other acute angle is 53° .

11. Use the diagrams below, please solve for x.

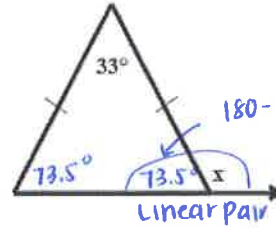
a.



$$133 = x + 62$$

$$x = 71$$

b.

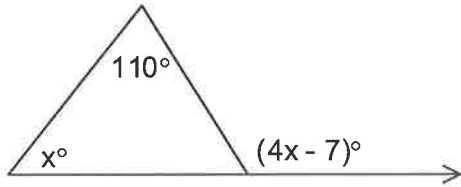


$$180 - 33 = 147 \div 2 \text{ base angles} = 73.5$$

$$x + 73.5 = 180$$

$$x = 106.5$$

12. Using the diagram below, please find the measure of the exterior angle.



$$4x - 7 = x + 110$$

$$3x - 7 = 110$$

$$3x = 117$$

$$x = 39$$

$$\text{Ext angle} = 4(39) - 7$$

$$= 149^\circ$$

13. If $m\angle PST = (x + 3y)^\circ$, $m\angle RPS = 45^\circ$, $m\angle PRS = 2y^\circ$, and $m\angle PSR = 5x^\circ$, find $m\angle PST$.

$$\Delta PRS: 2y + 5x + 45 = 180$$

$$2y + 5x = 135$$

$$\text{Linear Pair: } 5x + x + 3y = 180$$

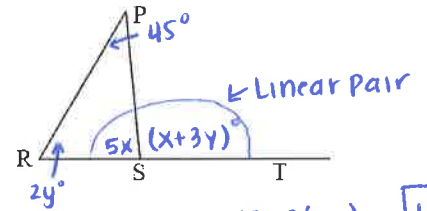
$$6x + 3y = 180$$

$$\text{System: } \begin{cases} 5x + 2y = 135 & \times 3 \\ 6x + 3y = 180 & \times -2 \end{cases} \Rightarrow \begin{matrix} 15x + 6y = 405 \\ -12x - 6y = -360 \\ \hline 3x = 45 \Rightarrow x = 15 \end{matrix}$$

$$5(15) + 2y = 135$$

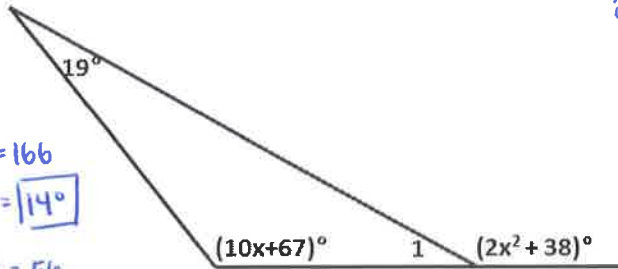
$$2y = 60$$

$$y = 30$$



$$m\angle PST = 15 + 3(30) = 105^\circ$$

14. Find all possibilities for $m\angle 1$ in the diagram below. (NOTE: Diagram not drawn to scale)



$$2x^2 + 38 = 10x + 67 + 19$$

$$2x^2 + 38 = 10x + 86$$

$$2x^2 - 10x - 48 = 0$$

$$\frac{2(x^2 - 5x - 24)}{2} = \frac{0}{2}$$

$$x^2 - 5x - 24 = 0$$

$$(x - 8)(x + 3) = 0 \Rightarrow x = 8 \text{ or } x = -3$$

Ext angle:

$$x = 8: 2(64) + 38 = 166$$

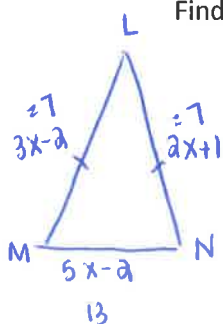
$$m\angle 1 = 180 - 166 = 14^\circ$$

$$x = -3: 2(9) + 38 = 56$$

$$m\angle 1 = 180 - 56 = 124^\circ$$

* 15. Given ΔLMN is isosceles, \overline{LN} and \overline{LM} are the legs, $LM = 3x - 2$, $LN = 2x + 1$, and $MN = 5x - 2$.

Find the value of x. and find the perimeter



$$3x - 2 = 2x + 1$$

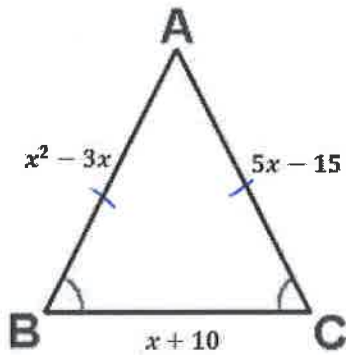
$$x - 2 = 1$$

$$x = 3$$

$$P = 7 + 7 + 13$$

$$P = 27 \text{ units}$$

16. Using the diagram below, find the value of x .



$$x^2 - 3x = 5x - 15$$

$$x^2 - 8x + 16 = 0$$

$$(x-5)(x-3) = 0$$

$$\boxed{x=5} \quad x=3$$

↑
not a
solution

check: $x=5$:

$$AB = 25 - 3(5) = 10$$

$$AC = 25 - 15 = 10 \quad \checkmark$$

$x=3$:

$$AB: 9 - 9 = 0$$

$$BC = 15 - 15 = 0$$

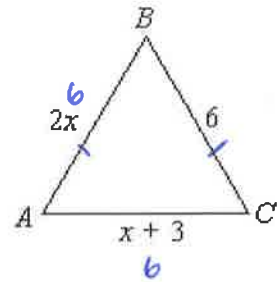
> can't have
zero side
lengths

17. Given that $\overline{AB} \cong \overline{BC}$, find the value of x and classify $\triangle ABC$ by its side lengths.

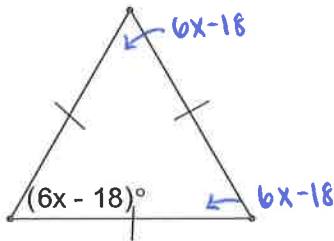
$$2x = 6$$

$$\boxed{x=3}$$

Equilateral \triangle



18. Given the diagram below, please find the value of x .



$$6x - 18 + 6x - 18 + 6x - 18 = 180$$

$$18x - 54 = 180$$

$$18x = 234$$

$$\boxed{x=13}$$

OR

$$6x - 18 = 60$$

$$6x = 78$$

$$\boxed{x=13}$$

19. Given the information listed in the diagram below, $m\angle BAE = 12^\circ$, $m\angle ABC = 52^\circ$, and $m\angle BCE = 26^\circ$, please find the values of x and y .

smaller \triangle : $y + 5y + x = 180$

$$6y + x = 180$$

Big \triangle : $5a + 1a + y + x + 26 = 180$

$$y + x + 90 = 180$$

$$y + x = 90$$

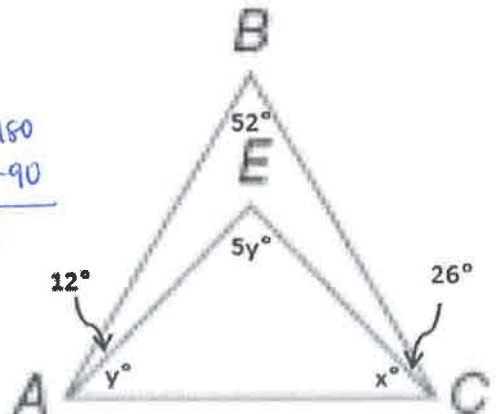
system: $\begin{cases} 6y + x = 180 \\ -(y + x = 90) \end{cases} \Rightarrow \begin{matrix} 6y + x = 180 \\ -y - x = -90 \\ \hline 5y = 90 \end{matrix}$

$$5y = 90$$

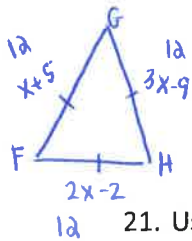
$$\boxed{y=18}$$

$$18 + x = 90$$

$$\boxed{x=72}$$



20. $\triangle FGH$ is equilateral with $FG = x + 5$, $GH = 3x - 9$, and $FH = 2x - 2$. Find the perimeter of $\triangle FGH$.



$$x + 5 = 2x - 2$$

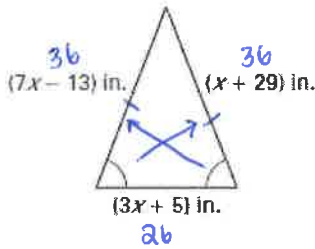
$$5 = x - 2$$

$$\boxed{x = 7}$$

$$P = 1d + 1d + 1d$$

$$\boxed{P = 36 \text{ units}}$$

21. Using the diagram below, please find perimeter of the triangle.



$$7x - 13 = x + 29$$

$$6x - 13 = 29$$

$$6x = 42$$

$$\boxed{x = 7}$$

$$P = 36 + 36 + 26$$

$$\boxed{P = 98 \text{ inches}}$$

A triangle has the given vertices. Graph the triangle, find each side length in simplest radical form, and classify the triangle by its side lengths. Determine if the triangle is a right triangle.

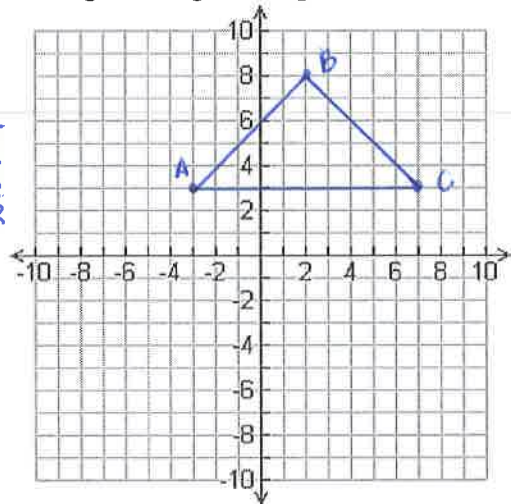
22. $A(-3, 3)$, $B(2, 8)$, $C(7, 3)$

$$AB = \sqrt{(2+3)^2 + (8-3)^2} = \sqrt{(5)^2 + (5)^2} = \sqrt{25+25} = \sqrt{50} = 5\sqrt{2}$$

$$BC = \sqrt{(7-2)^2 + (3-8)^2} = \sqrt{(5)^2 + (-5)^2} = \sqrt{25+25} = \sqrt{50} = 5\sqrt{2}$$

$$AC = \sqrt{(7+3)^2 + (3-3)^2} = \sqrt{(10)^2 + (0)^2} = \sqrt{100} = 10$$

Isosceles



$$m_{\overline{AB}} = \frac{8-3}{2+3} = \frac{5}{5} = 1$$

$$m_{\overline{BC}} = \frac{3-8}{7-2} = \frac{-5}{5} = -1$$

Since $\overline{AB} \perp \overline{BC}$, $\triangle ABC$ is a right triangle

$$m_{\overline{AC}} = \frac{3-3}{7+3} = \frac{0}{10} = 0$$

Right Isosceles

23. $D(1, 1)$, $E(4, 0)$, $F(8, 5)$

$$DE = \sqrt{(4-1)^2 + (0-1)^2} = \sqrt{(3)^2 + (-1)^2} = \sqrt{9+1} = \sqrt{10}$$

$$EF = \sqrt{(8-4)^2 + (5-0)^2} = \sqrt{(4)^2 + (5)^2} = \sqrt{16+25} = \sqrt{41}$$

$$FD = \sqrt{(8-1)^2 + (5-1)^2} = \sqrt{(7)^2 + (6)^2} = \sqrt{49+36} = \sqrt{85}$$

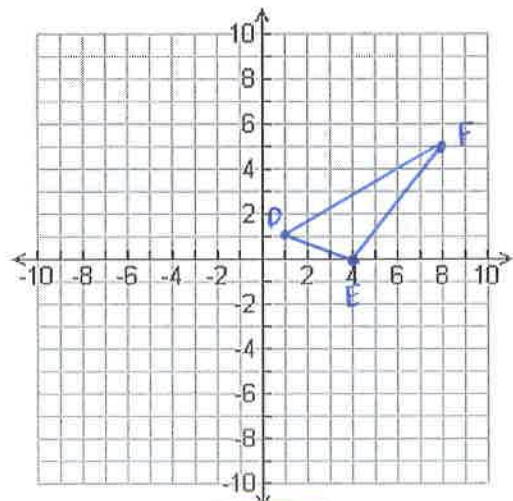
Scalene

$$m_{\overline{DE}} = \frac{0-1}{4-1} = \frac{-1}{3}$$

$$m_{\overline{EF}} = \frac{5-0}{8-4} = \frac{5}{4}$$

$$m_{\overline{FD}} = \frac{5-1}{8-1} = \frac{4}{7}$$

since none of the slopes are opp. reciprocals, $\triangle DEF$ is not a right triangle



Scalene Non-Right

24. G(1, -3), H(2, -6), I(-1, -5)

$$GH = \sqrt{(2-1)^2 + (-6+3)^2} = \sqrt{(1)^2 + (-3)^2} = \sqrt{1+9} = \sqrt{10}$$

$$HI = \sqrt{(-1-2)^2 + (-5+6)^2} = \sqrt{(-3)^2 + (1)^2} = \sqrt{9+1} = \sqrt{10}$$

$$IG = \sqrt{(-1-1)^2 + (-5+3)^2} = \sqrt{(-2)^2 + (-2)^2} = \sqrt{4+4} = \sqrt{8} = 2\sqrt{2}$$

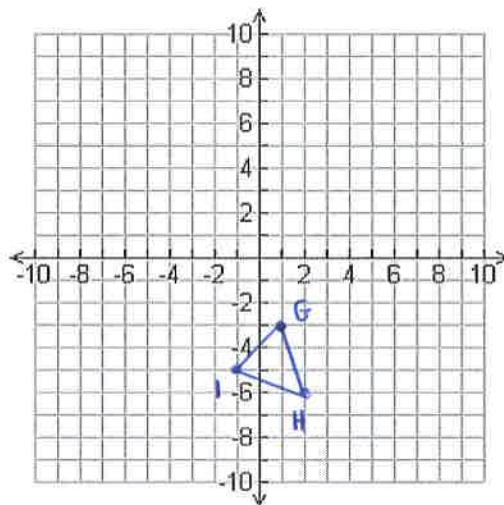
Isosceles

$$m_{\overline{GH}} = \frac{-6+3}{2-1} = \frac{-3}{1} = -3$$

$$m_{\overline{HI}} = \frac{-5+6}{-1-2} = \frac{1}{-3} = -\frac{1}{3}$$

$$m_{\overline{IG}} = \frac{-5+3}{-1-1} = \frac{-2}{-2} = 1$$

Since none of the slopes are opp. reciprocals, $\triangle GHI$ is not a right triangle



Isosceles Non-Right

25. J(0, 0), K(6, 0), L(3, $\sqrt{27}$)

$$JL = \sqrt{(3-0)^2 + (\sqrt{27}-0)^2} = \sqrt{(3)^2 + (\sqrt{27})^2} = \sqrt{9+27} = \sqrt{36} = 6$$

$$LK = \sqrt{(3-6)^2 + (\sqrt{27}-0)^2} = \sqrt{(-3)^2 + (\sqrt{27})^2} = \sqrt{9+27} = \sqrt{36} = 6$$

$$JK = \sqrt{(6-0)^2 + (0-0)^2} = \sqrt{(6)^2} = \sqrt{36} = 6$$

Equilateral

$$m_{\overline{JL}} = \frac{\sqrt{27}-0}{3-0} = \frac{\sqrt{27}}{3}$$

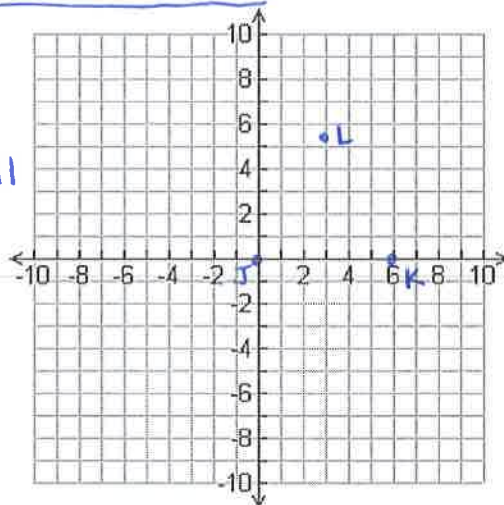
$$m_{\overline{LK}} = \frac{\sqrt{27}-0}{3-6} = \frac{-\sqrt{27}}{3}$$

$$m_{\overline{JK}} = \frac{0-0}{6-0} = \frac{0}{6} = 0$$

Since none of the slopes are opp. reciprocals, $\triangle JKL$ is not a right triangle.

It could never be a right \triangle since all angles have measures of 60° in an equilateral triangle

Equilateral



Answer Key :

- 1) a. True, each angle in an equilateral triangle is always 60°
 - b. False, if a triangle had more than one obtuse angle, the interior angle sum would be greater than 180°
 - c. False, an angle would have to have two obtuse angles in order to have two acute exterior angles
 - d. True, if a triangle had more than one right angle, the interior angle sum would be greater than 180°
- 2) $x = 8$, right triangle
- 3) Scalene triangle
- 4) $m\angle 1 = 104^\circ$, $m\angle 2 = 76^\circ$, $m\angle 3 = 42^\circ$, $m\angle 4 = 48^\circ$, $m\angle 5 = 49^\circ$
- 5) $m\angle 1 = 140^\circ$, $m\angle 2 = 40^\circ$, $m\angle 3 = 65^\circ$, $m\angle 4 = 75^\circ$, $m\angle 5 = 115^\circ$
- 6) $x = 30$, $y = 60$
- 7) Angles : 34° , 136° , 10° , Obtuse Scalene
- 8) $m\angle 1 = 112^\circ$, $m\angle 2 = 68^\circ$, $m\angle 3 = 43^\circ$, $m\angle 4 = 137^\circ$, $m\angle 5 = 69^\circ$, $m\angle 6 = 111^\circ$, $m\angle 7 = 69^\circ$
- 9) $m\angle ACB = 40^\circ$, $m\angle AFB = 140^\circ$
- 10) 53°
- 11) a. $x = 71$ b. $x = 106.5$
- 12) 149°
- 13) $x = 15$, $y = 30$, $m\angle PST = 105^\circ$
- 14) $m\angle 1 = 14^\circ$, OR $m\angle 1 = 124^\circ$
- 15) $x = 3$
- 16) $x = 5$
- 17) $x = 3$, Equilateral
- 18) $x = 13$
- 19) $x = 72$, $y = 18$
- 20) $P = 36$ units
- 21) $P = 98$ inches
- 22) Right Isosceles Triangle
- 23) Obtuse Scalene Triangle
- 24) Acute Isosceles Triangle
- 25) Equilateral Triangle