

You should be able to...

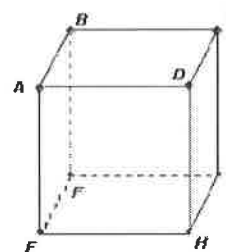
- ✓ Identify parallel, perpendicular and skew lines. Identify parallel and perpendicular planes. **(Section 3.1)**
- ✓ Identify corresponding angles, alternate interior angles, consecutive interior angles, and alternate exterior angles. **(Section 3.1)**
- ✓ Find measure of angles formed by parallel lines intersected by a transversal (Corresponding Angles Postulate, Alternate Interior Angles Theorem, Alternate Exterior Angles Theorem, Consecutive Interior Angles Theorem). **(Section 3.2)**
- ✓ Prove lines are parallel (Corresponding Angles Converse, Alternate Interior Angles Converse, Alternate Exterior Angles Converse, Consecutive Interior Angles Converse) **(Section 3.3)**

Practice Problems

1. Two lines that are not coplanar and do not intersect are called _____.

- a. Parallel b. Perpendicular **c. Skew** d. None of the above

Use the diagram of the cube to the right for questions #2 – 4 below.



2. \overrightarrow{AD} and \overrightarrow{HG} are _____.

- a. Parallel lines b. Perpendicular Lines **c. Skew Lines** d. None

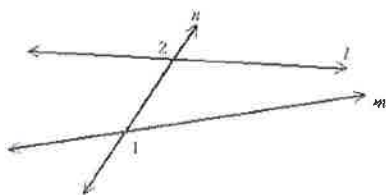
3. \overrightarrow{BC} and \overrightarrow{AB} are _____.

- a. Parallel lines **b. Perpendicular Lines** c. Skew Lines d. None

4. \overrightarrow{FB} and \overrightarrow{GC} are _____.

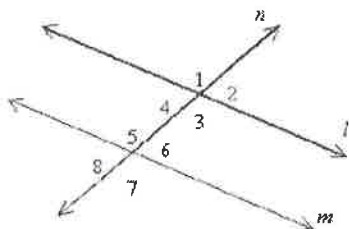
- a. Parallel lines** b. Perpendicular Lines c. Skew Lines d. None

5. In the figure below, $\angle 1$ and $\angle 2$ are _____.



- a. Alternate exterior angles
- b. Alternate interior angles
- c. Consecutive interior angles
- d. Corresponding angles

Use the following figure to answer questions 18 – 19.



6. In the figure above, $\angle 6$ and $\angle 3$ are _____.

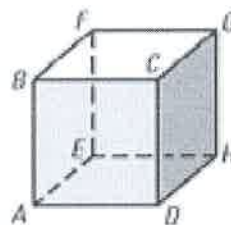
- a. Alternate exterior angles
- b. Consecutive interior angles
- c. Corresponding angles
- d. Alternate interior angles

7. In the figure above, $\angle 6$ and $\angle 2$ are _____.

- a. Alternate interior angles
- b. Consecutive interior angles
- c. Alternate exterior angles
- d. Corresponding angles

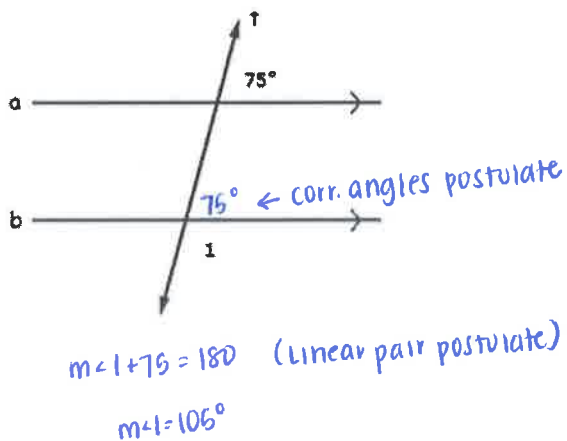
8. Using the diagram below, name **FOUR** pairs of perpendicular lines in the figure.

- ① $\overleftrightarrow{AB}, \overleftrightarrow{BC}$
- ② $\overleftrightarrow{FG}, \overleftrightarrow{FE}$
- ③ $\overleftrightarrow{AE}, \overleftrightarrow{EH}$
- ④ $\overleftrightarrow{CD}, \overleftrightarrow{AD}$



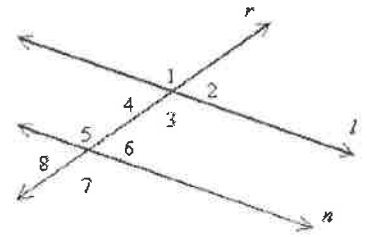
9. Find $m\angle 1$ in the figure below given that $\overleftrightarrow{PQ} \parallel \overleftrightarrow{RS}$.

- a. 105°
- b. 75°
- c. 115°
- d. 15°



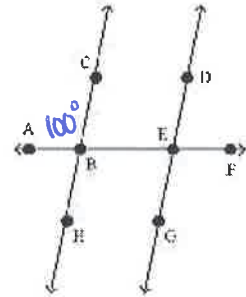
10. In the figure below, $l \parallel n$ and r is a transversal. Which of the following is **not** necessarily true?

- a. $\angle 8 \cong \angle 2$
- b. $\angle 2 \cong \angle 6$
- c. $\angle 5 \cong \angle 3$
- d. $\angle 4 \cong \angle 7$**



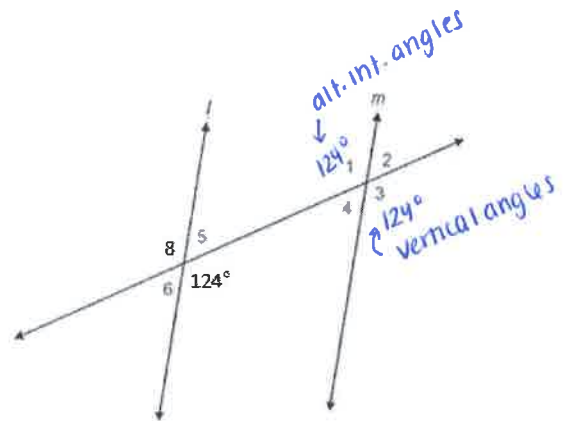
11. In the figure shown, $\overline{HC} \parallel \overline{GD}$ and $m\angle ABC = 100^\circ$. Which of the following statements is false?

- ~~a. $m\angle CBE = 80^\circ$~~
- ~~b. $m\angle DEF = 80^\circ$~~
- c. $\angle DEB$ and $\angle CBE$ are corresponding angles**
- ~~d. $\angle CBE$ and $\angle GEB$ are alternate interior angles~~



12. Use the figure to find the measure of $\angle 3$.

- a. 124°**
- b. 56°
- c. 79°
- d. 146°



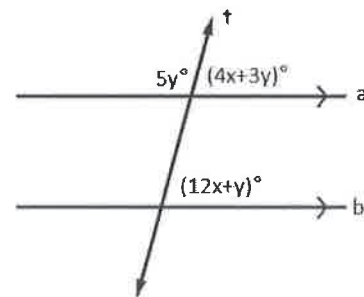
13. Please find the values of x and y . Justify each step using the appropriate theorem/postulate.

$$\begin{aligned} 5y + 4x + 3y &= 180 & 4x + 3y &= 12x + y \\ \rightarrow 4x + 8y &= 180 & \rightarrow -8x + 2y &= 0 \end{aligned}$$

$$\begin{aligned} \text{System: } \begin{cases} 4x + 8y = 180 \\ -4(-8x + 2y = 0) \end{cases} &\Rightarrow \begin{aligned} 4x + 8y &= 180 \\ 32x - 8y &= 0 \end{aligned} \\ \hline &36x = 180 \end{aligned}$$

$$\boxed{x = 5}$$

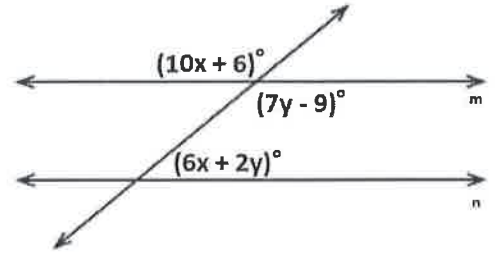
$$\begin{aligned} 4(5) + 8y &= 180 \\ 20 + 8y &= 180 \\ 8y &= 160 \Rightarrow \boxed{y = 20} \end{aligned}$$



14. Given $m \parallel n$, please find the values of x and y . Justify each step using the appropriate theorem/postulate.

$10x+6=7y-9$ (vertical angles thm)
 $\rightarrow 10x-7y=-15$
 $7y-9+6x+2y=180$
 $\rightarrow 6x+9y=189$

System: $\begin{cases} 10x-7y=-15 \\ -10(6x+9y=189) \end{cases}$
 $\Rightarrow 60x-42y=-90$
 $-60x-90y=-1890$
 $-132y=-1980$
 $y=15$



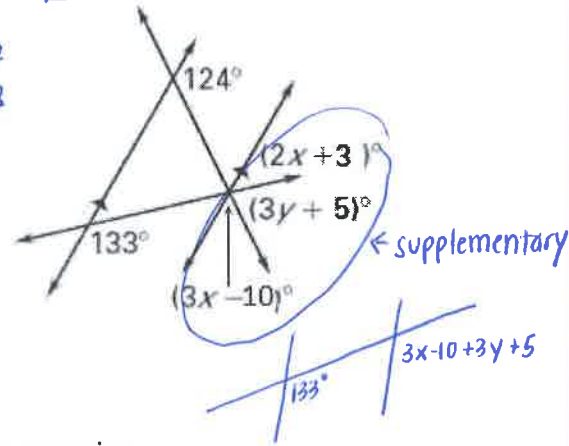
$10x-7(15)=-15$
 $10x-105=-15$
 $10x=90 \Rightarrow x=9$

15. Given the diagram below, please solve for x and y .

$2x+3+3y+5+3x-10=180$
 $5x+3y-2=180$
 $\rightarrow 5x+3y=182$
 $133=3x-10+3y+5$
 $133=3x+3y-5$
 $\rightarrow 3x+3y=138$

System: $\begin{cases} 5x+3y=182 \\ -1(3x+3y=138) \end{cases} \Rightarrow \begin{cases} 5x+3y=182 \\ -3x-3y=-138 \end{cases}$
 $2x=44$
 $x=22$

$3(22)+3y=138$
 $66+3y=138$
 $3y=72$
 $y=24$



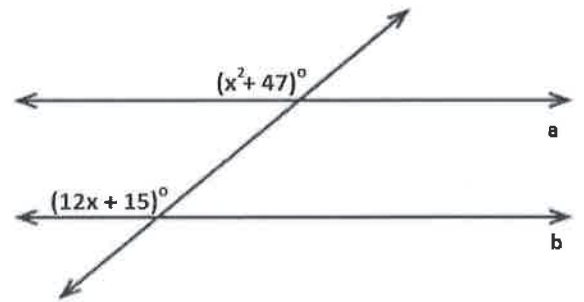
16. Please find the value of x that will make $a \parallel b$. Please justify your reasoning.

$x^2+47=12x+15$
 $x^2-12x+47-15=0$
 $x^2-12x+32=0$
 $(x-4)(x-8)=0$

$x=4, x=8$

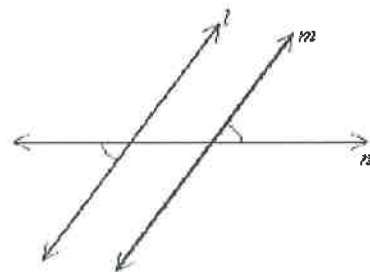
both solutions work by corresponding angles converse

check:
 $x=4: (4)^2+47=63^\circ$
 $12(4)+15=63^\circ$
 $x=8: (8)^2+47=111^\circ$
 $12(8)+15=111^\circ$



17. Using the figure below, which theorem guarantees l and m are parallel?

- a. Alternate Interior Angles Converse
- b. Consecutive Interior Angles Converse
- c. Corresponding Angles Converse
- d. Alternate Exterior Angles Converse



18. Find the value of x that will allow you to prove that $\overleftrightarrow{CD} \parallel \overleftrightarrow{EF}$ if $m\angle 1 = (3x + 30)^\circ$ and $m\angle 2 = 81^\circ$.

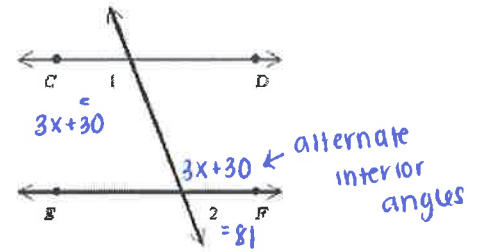
State which theorem or postulate you used for each step.

$$3x + 30 + 81 = 180 \quad (\text{Linear pair postulate})$$

$$3x + 111 = 180 \quad (\text{combine like terms})$$

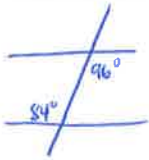
$$3x = 69 \quad (\text{subtraction property})$$

$$\boxed{x = 23} \quad (\text{division property})$$

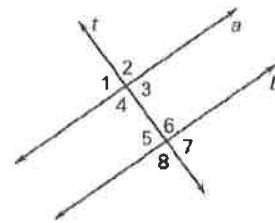


Use the following given angle measures to decide whether lines a and b are parallel. Explain.

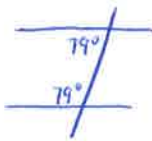
19. $m\angle 3 = 96^\circ$, $m\angle 5 = 84^\circ$



No, the lines are not parallel because $\angle 3$ would have to be congruent to $\angle 5$ by the alt. interior angles converse

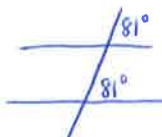


20. $m\angle 5 = 79^\circ$, $m\angle 4 = 79^\circ$



No, the lines would not be parallel because $\angle 5 + \angle 4 = 180$ in order for the lines to be parallel by the consec. interior angles converse

21. $m\angle 2 = 81^\circ$, $m\angle 6 = 81^\circ$



Yes, the lines are parallel since $\angle 2 \cong \angle 6$. Because $\angle 2 \cong \angle 6$ by corresponding angles converse, then $a \parallel b$.

True or False:

22. If two parallel lines are intersected by a transversal, then alternate exterior angles have measures of 90 degrees. **False** - alt. ext angles must have congruent measures

23. If two parallel lines are intersected by a transversal, then consecutive interior angles are supplementary. **True**

24. If two lines are intersected by a transversal and alternate interior angles are equal in measure, then the lines are parallel. **True**

25. If two lines are intersected by a transversal and corresponding angles are supplementary, then the lines are parallel. **False** - corresponding angles must have congruent measures

Answer Key :

1. C ✓
2. C ✓
3. B ✓
4. A ✓
5. A ✓
6. B ✓
7. D ✓
8. Sample answer: \overrightarrow{AB} and \overrightarrow{BC} , \overrightarrow{AB} and \overrightarrow{AD} , \overrightarrow{FG} and \overrightarrow{GH} , \overrightarrow{GH} and \overrightarrow{DH} ✓
9. A ✓
10. D ✓
11. C ✓
12. A ✓
13. $x = 5, y = 20$ ✓
Sample answer : $4x + 3y = 12x + y$ Corresponding Angles Postulate
 $5y + 4x + 3y = 180$ Linear Pair Postulate
14. $x = 9, y = 15$ ✓
Sample answer: $10x + 6 = 7y - 9$ Vertical Angles Theorem
 $7y - 9 + 6x + 2y = 180$ Consecutive Interior Angles Theorem
15. $x = 22, y = 24$ ✓
16. $x = 4$ or $x = 8$, Corresponding Angles Converse ✓
17. D ✓
18. The angle next to $\angle 1$ is also 81° because of corresponding angles.
 $\angle 1 + 81 = 180$ because they make a linear pair (are supplementary)
 $3x + 30 + 81 = 180$ by substitution
 $x = 23$ ✓
19. Line a and line b are not parallel. ✓
In order to be parallel, $\angle 3 \cong \angle 5$ by the alternate interior angles converse
20. Line a and line b are not parallel. ✓
In order to be parallel, $m\angle 4 + m\angle 5 = 180$ by the consecutive interior angles converse
21. Line a and line b are parallel because $\angle 2 \cong \angle 6$ by the corresponding angles converse ✓
22. False – Alternate exterior angles have to have the same measure ✓
23. True – By the consecutive interior angles converse ✓
24. True – By the alternate interior angles converse ✓
25. False – Corresponding angles must have the same measure ✓