Geometry A

4.4: Prove Triangles Congruent by H-L

Name: \_\_\_\_\_\_ Date: \_\_\_\_\_\_ Period: \_\_\_\_\_



I can prove triangles congruent using H-L

### Vocabulary:

In a right triangle, the side opposite the right angle is called the \_\_\_\_\_\_.

In a right triangle, the sides that form the right angle are called the \_\_\_\_\_\_.

In right triangle <i>ABC</i> , the hypotenuse is	A B
The legs are and	
	, c

There is a special method for proving right triangles are congruent. This method only works for right triangles!

Hypotenuse – Leg Theorem (H-L)	Example:	В	E
If the hypotenuse and leg of one right triangle are congruent to the hypotenuse and leg of a second right triangle, then the two triangles are congruent.	If <b>Hypotenuse</b> $\overline{BC} \cong$ and <b>Leg</b> $\overline{AB} \cong$ in right triangles $\triangle ABC$ and $\triangle DEF$ , then $A$ $\triangle ABC \cong$		

## Example 1: Using H-L to identify congruent triangles

Can you prove the following triangles are congruent? Explain.







d.



When writing a proof using H-L, it is important that you state the following three things in your explanation:

- That the two triangles are right triangles.
- One pair of legs is congruent.
- $\circ$   $\;$  The two hypotenuse are congruent.

## Example 2: Proofs involving H-L

a) **Given:**  $\overline{AC} \cong \overline{EC}$ ;  $\overline{AB} \perp \overline{BD}$ ;  $\overline{ED} \perp \overline{BD}$ ;  $\overline{AC}$  is a bisector of  $\overline{BD}$ 

**Prove:**  $\triangle ABC \cong \triangle EDC$ 



Statements	Reasons
<b>1.</b> $\overline{AC} \cong \overline{EC}$	1.
<b>2.</b> $\overline{AB} \perp \overline{BD}; \overline{ED} \perp \overline{BD}$	2.
3.	3.
4.	4.
<b>5.</b> $\overline{AC}$ is a bisector of $\overline{BD}$	5.
<b>6.</b> <i>BC</i> ≅	6.
<b>7.</b> $\triangle ABC \cong \triangle EDC$	7.

b) Given:  $\overline{AB} \cong \overline{DC}$ ;  $\overline{BA} \perp \overline{AC}$ ;  $\overline{CD} \perp \overline{DB}$ Prove:  $\triangle ABC \cong \triangle DCB$ 



	B D
Statements	Reasons
<b>1.</b> $\overline{AB} \cong \overline{DC}$	1.
<b>2.</b> $\overline{BA} \perp \overline{AC}; \overline{CD} \perp \overline{DB}$	2.
<b>3.</b> $\angle A$ and $\angle D$ are	3.
<b>4.</b> $\triangle ABC and \triangle EDC$ are	4.
<b>5.</b> $\overline{CB} \cong \overline{CB}$	5.
<b>6.</b> $\triangle ABC \cong \triangle DCB$	6.

# Does a right angle always mean we will use H-L? Let's see!

**Given:**  $\overline{AB}$  is perpendicular bisector of  $\overline{CD}$ **Prove:**  $\triangle ABC \cong \triangle ABD$ 



Statements	Reasons
<b>1.</b> $\overline{AB}$ is perpendicular bisector of $\overline{CD}$	1.
2.	2. definition of perpendicular lines
<b>3.</b> ∠ABC≅∠ABD	3.
<b>4.</b> <i>BC</i> ≅	4.
<b>5.</b> $\overline{AB} \cong \overline{AB}$	5.
<b>6.</b> $\triangle ABC \cong \triangle ABD$	6.

Geometry A Homework: H-L

Name:	
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### Is it possible to prove that the triangles are congruent? If so, state the postulate or theorem you would use.

State the third congruence that is needed to prove that  $\triangle ABC \cong \triangle XYZ$  using the given postulate or theorem.

**7. GIVEN:**  $\angle B \cong \angle E, \overline{BC} \cong \overline{EF}, \underline{\qquad} \cong \underline{\qquad}$ Use the SAS Congruence Theorem

8. GIVEN:  $\overline{AB} \cong \overline{DE}$ ,  $\overline{BC} \cong \overline{EF}$ , \_\_\_\_\_  $\cong$  \_\_\_\_\_ Use the SSS Congruence Postulate



9. GIVEN:  $\overrightarrow{AC} \cong \overrightarrow{DF}$ ,  $\angle A$  is a right angle and  $\angle A \cong \angle D$ ,  $\underline{\qquad} \cong \underline{\qquad}$ 

Use the H-L Congruence Theorem

10. Complete the proof.	$\bigwedge^{o}$
Given: $\overline{OM} \perp \overline{LN}$ , $\overline{ML} \cong \overline{MN}$	
<b>Prove:</b> $\triangle OML \cong \triangle OMN$	
Statements	Reasons
$1\overline{OM} \perp \overline{LN}$	1.
2. $\angle LMO$ and $\angle NMO$ are right angles	2. def. of
3. $\Delta LMO$ and $\Delta NMO$ are right triangles	3. Def. of
4. $\overline{ML} \cong \overline{MN}$	4.
5.	5. Reflexive Property
3. $\Delta OML \cong \Delta OMN$	6.

11. Given:  $\angle$  JKL &  $\angle$  MLK are right angles

 $\overline{JL} \cong \overline{MK}$  **Prove:**  $\Delta JKL \cong \Delta MLK$ 



Statements	Reasons
<b>1.</b> ∠ <i>JKL</i> & ∠ <i>MLK</i> are right ∠s	1.
2. $\Delta JKL and \Delta MLK$ are	2.
<b>3.</b> $\overline{JL} \cong \overline{MK}$	3.
$4.  \overline{KL} \cong \overline{KL}$	4.
5. $\Delta JKL \cong \Delta MLK$	5.

12. Given:  $\overline{AB} \cong \overline{DB}$ ,  $\overline{BC} \perp \overline{AD}$ 

**Prove:**  $\triangle ABC \cong \triangle DBC$ 



Statements	Reasons
<b>1.</b> $\overline{AB} \cong \overline{DB}$	1.
<b>2.</b> $\overline{BC} \perp \overline{AD}$	2.
<b>3.</b> ∠BCA and ∠BCD are	3.
<b>4.</b> ΔABC and ΔDBC are	4.
<b>5.</b> $\overline{CB} \cong \overline{CB}$	5.
$6.  \Delta ABC \cong \Delta DCB$	6.

#### Answer Key:

- 1. Yes, by SAS
- 2. Yes, by AAS
- 3. Yes, by SAS
- 4. Yes, by SAS
- 5. Yes, by SAS
- 6. Yes, by H-L
- 7.  $\overline{BA} \cong \overline{ED}$
- 8.  $\overline{AC} \cong \overline{DF}$
- 9.  $\overline{BC} \cong \overline{EF}$
- 10. 1) Given 2) Def of Perpendicular Lines 3) Def of right triangles 4)  $\overline{OM} \cong \overline{OM}$  5) SAS
- 11. 1) Given 2) Right triangles; Def of right triangles 3) Given 4) Reflexive Property 5) H-L
- 12. 1) Given 2) Given 3) Right angles; Def of perpendicular lines 4) Right triangles; Def of right triangles5) Reflexive Property 6) H-L