



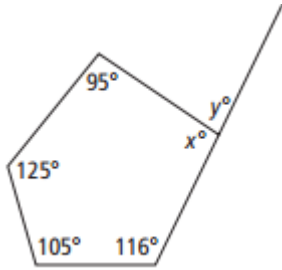
- I can find angle measures in polygons.
- I can use properties of parallelograms to find side lengths and angle measures.
- I can use properties to identify parallelograms.
- I can use coordinate geometry to identify parallelograms.

**I can find angle measures in polygons.**

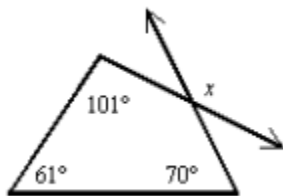
- ✓ I can find the sum of interior angles of a polygon using  $(n - 2) \cdot 180$
- ✓ I can find the measure of each interior angle of a regular polygon using  $\frac{(n - 2) \cdot 180}{n}$
- ✓ I can find the sum of the exterior angles of a polygon using 360
- ✓ I can find the measure of each exterior angle of a polygon using  $\frac{360}{n}$

1) What is the sum of the interior angle measures of a 15-gon?

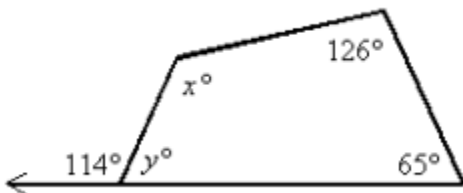
2) Find the values of the variables in the figure below.



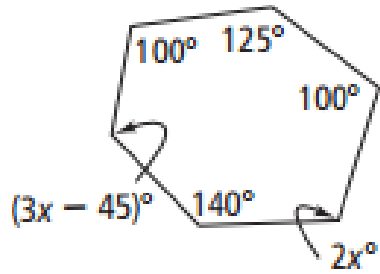
3) Find the value of x.



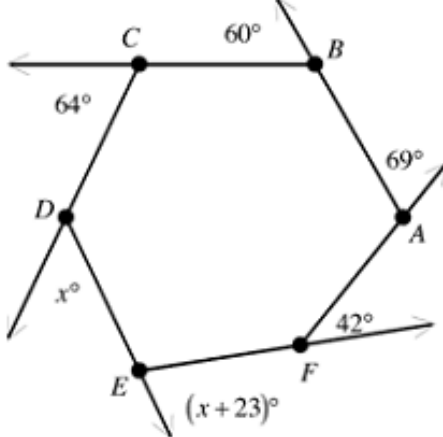
4) Find the values of x and y.



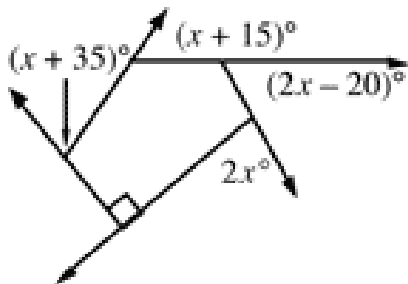
5) Find the value of  $x$ .



6) Find the value of  $x$ .



7) Find the value of  $x$ .



8) What is the measure of each interior and each exterior angle of a regular decagon?

9) Find the number of sides of a convex polygon if the sum of the measures of its interior angles is  $2880^\circ$ .

10) Find the number of sides of a regular polygon with each interior angle equal to  $171^\circ$ .

11) You are designing patterns for your art project. Can you form regular polygons with the given interior angle measures? If yes, how many sides would the regular polygon have?

a)  $135^\circ$

b)  $130^\circ$

**I can use properties of parallelograms to find side lengths and angle measures.**

- ✓ I can find lengths of opposite sides on parallelograms.
- ✓ I can find measures of opposite angles in parallelograms.
- ✓ I can find measures of consecutive angles in parallelograms.
- ✓ I can find lengths of diagonals in parallelograms.
- ✓ I can use properties of parallel lines to find angle measures in parallelograms.

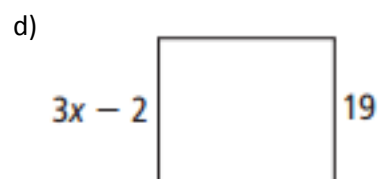
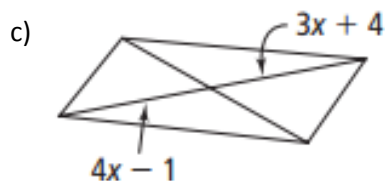
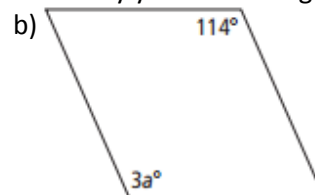
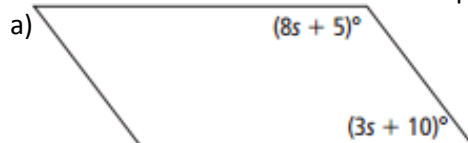
12) Consecutive angles in a parallelogram are always\_\_\_\_\_.

- A) Congruent angles.
- B) Complementary angles.
- C) Supplementary angles.
- D) Vertical angles.

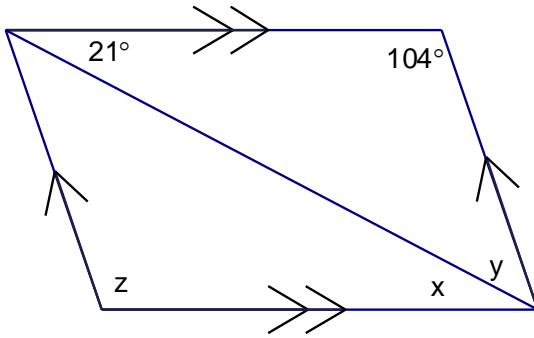
13) Choose the statement that is NOT ALWAYS true. For any parallelogram\_\_\_\_\_.

- A) The diagonals bisect each other.
- B) Opposite angles are congruent.
- C) The diagonals are perpendicular.
- D) Opposite sides are congruent.

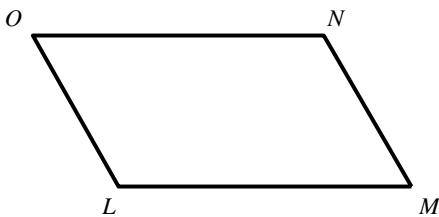
14) Find the value of the variable in each parallelogram below. Justify your reasoning.



15) Find the values of the variables in the parallelogram.

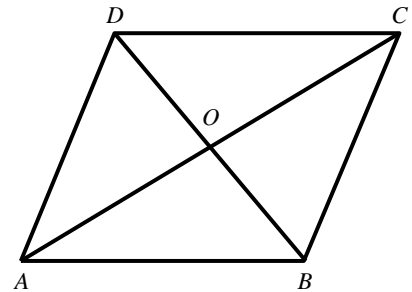


16) If  $ON = 7x - 5$ ,  $LM = 6x + 3$ ,  $NM = x - 4$ , and  $OL = 2y + 5$ , find the values of  $x$  and  $y$  given that  $LMNO$  is a parallelogram.

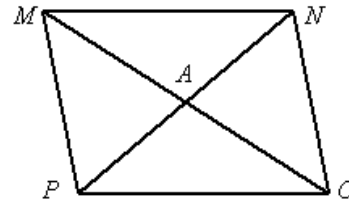


17) Complete each statement for parallelogram  $ABCD$ . Then justify your answer.

- A)  $\overline{AD} \cong$  \_\_\_\_\_
- B)  $\overline{OC} \cong$  \_\_\_\_\_
- C)  $\overline{CD} \cong$  \_\_\_\_\_
- D)  $\angle CBA \cong$  \_\_\_\_\_

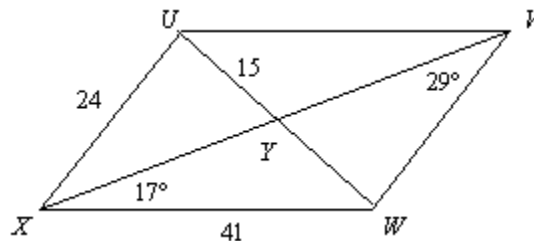


18) Find  $AM$  in the parallelogram if  $PN = 10$  and  $MO = 19$ .

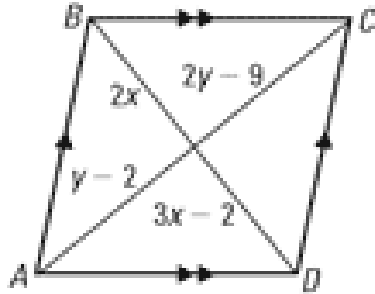


19) Use the diagram below to find each of the following.

- a)  $m\angle WVU =$  \_\_\_\_\_
- b)  $WV =$  \_\_\_\_\_
- c)  $m\angle XUV =$  \_\_\_\_\_
- d)  $UW =$  \_\_\_\_\_

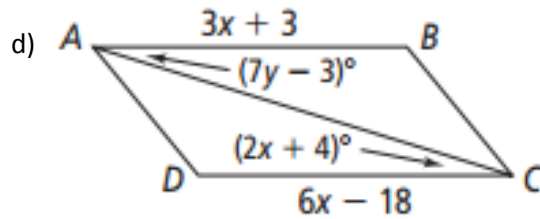
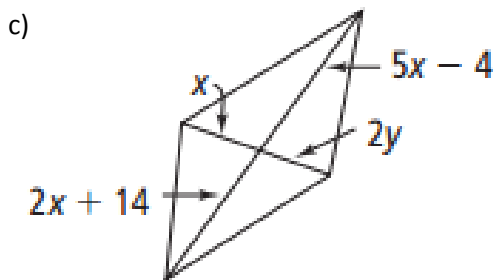
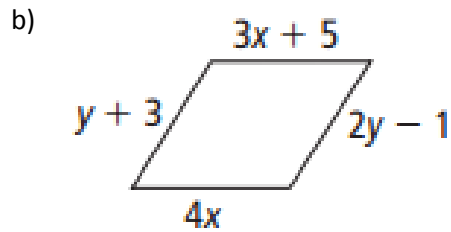
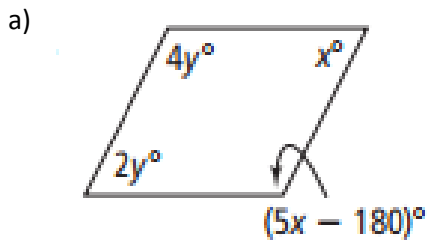


20) In the diagram below, please find  $AC$  and  $BD$ .

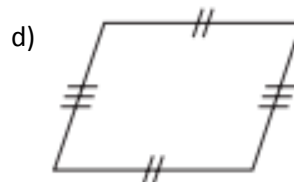
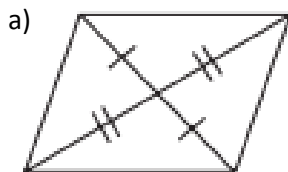


□ I can use properties to identify parallelograms.

21) In each of the following, for what values of  $x$  and  $y$  must each figure be a parallelogram. Explain.

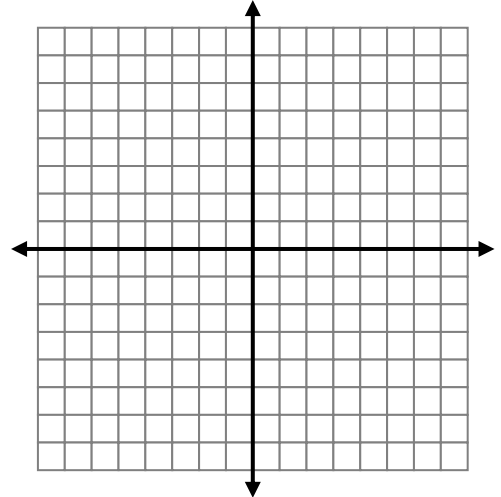


22) Can you prove that the quadrilateral is a parallelogram based on the given information? Explain.

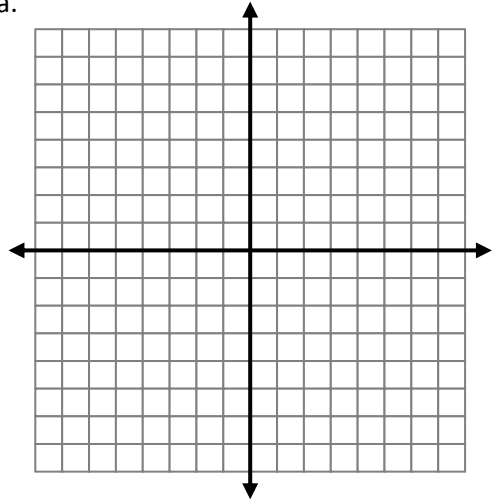


□ I can use coordinate geometry to identify parallelograms in the coordinate plane.

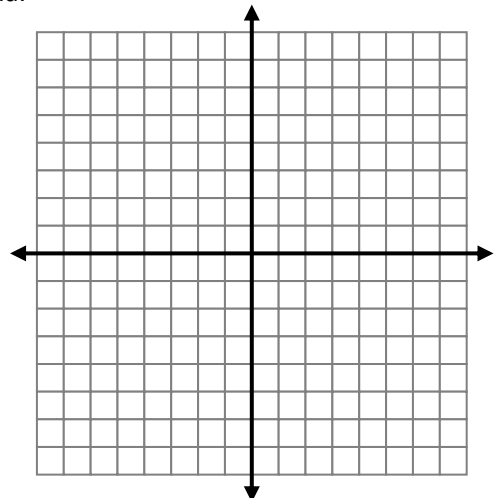
23) Given: Quadrilateral ABCD with  $A(-5, 0)$ ,  $B(4, -3)$ ,  $C(8, -1)$  and  $D(-1, 2)$ .  
Prove: ABCD is a parallelogram using the slope formula.



24) Given: Quadrilateral ABCD with  $A(-5, -5)$ ,  $B(-2, 4)$ ,  $C(6, 4)$  and  $D(3, -5)$ .  
Prove: ABCD is a parallelogram using the distance formula.



25) Given: Quadrilateral ABCD with  $A(-2, 3)$ ,  $B(3, 2)$ ,  $C(2, -1)$  and  $D(-3, 0)$ .  
Prove: ABCD is a parallelogram using the midpoint formula.



## ANSWER KEY

- 1) 2340
- 2)  $X = 99, y = 81$
- 3)  $X = 128$
- 4)  $X = 103, y = 66$
- 5)  $X = 60$
- 6)  $X = 51$
- 7)  $X = 40$
- 8) Each interior angle measures  $144^\circ$ , each exterior angle measures  $36^\circ$
- 9) 18
- 10) 40
- 11) a) Yes, it has 8 sides    b) no, a regular polygon cannot be formed.
- 12) C
- 13) C
- 14) a)  $S = 15$ ; In a parallelogram, consecutive angles are supplementary  
b)  $A = 38$ , in a parallelogram, opposite angles are congruent  
c)  $X = 5$ ; in a parallelogram, diagonals bisect each other  
d)  $X = 7$ ; in a parallelogram, opposite sides are congruent
- 15)  $X = 21, y = 55, z = 104$
- 16)  $X = 8, y = -1/2$
- 17) a)  $\overline{BC}$ ; in a parallelogram, opposite sides are congruent  
b)  $\overline{AO}$ ; in a parallelogram, diagonals bisect each other  
c)  $\overline{AB}$ ; in a parallelogram, opposite sides are parallel (definition of parallelogram)  
d)  $\angle ADC$ , in a parallelogram, opposite angles are congruent
- 18)  $AM = 9.5$
- 19) a)  $46^\circ$   
b) 24  
c)  $134^\circ$   
d) 30
- 20)  $AC = 10, BD = 8$
- 21) a)  $x = 60, y = 30$ ; For a quadrilateral to be a parallelogram, consecutive angles must be supplementary  
b)  $x = 5, y = 4$ ; For a quadrilateral to be a parallelogram, opposite sides must be congruent  
c)  $x = 6, y = 3$ ; For a quadrilateral to be a parallelogram, diagonals must bisect each other  
d)  $x = 7, y = 3$ ; For a quadrilateral to be a parallelogram, one pair of opposite sides must be both congruent and parallel
- 22) a) yes, the diagonals bisect each other  
b) No, not enough information  
c) yes, the missing angle measures  $44^\circ$ , so opposite angles are congruent  
d) yes, opposite sides are congruent
- 23)  $\text{slope of } \overline{AD} = \text{slope of } \overline{BC} = \frac{1}{2} \Rightarrow \overline{AD} \parallel \overline{BC}$ ;  $\text{slope of } \overline{AB} = \text{slope of } \overline{CD} = -\frac{1}{3} \Rightarrow \overline{AB} \parallel \overline{CD}$   
Opposite sides are parallel, so ABCD is a parallelogram
- 24)  $AB = CD = \sqrt{90}$ ;  $AD = BC = 8$ ; Opposite sides are congruent, so ABCD is a parallelogram
- 25) Midpoint of  $\overline{AC}$  is (0, 1); Midpoint of  $\overline{BD}$  is (0, 1). Since  $\overline{AC}$  and  $\overline{BD}$  have same midpoint, the diagonals bisect each other.