



- I can classify triangles on the coordinate plane using slope and distance formulas.

Recall:

Slope formula: $m = \frac{y_2 - y_1}{x_2 - x_1}$

Distance formula: $d = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

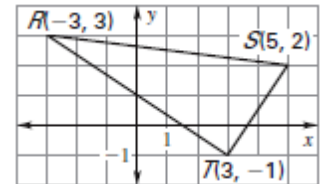
Two lines on the coordinate plane are **perpendicular** if _____.

To classify triangles on the coordinate plane:

- Use the distance formula to find the length of each side of the triangle.
 - If no sides are congruent, the triangle is _____.
 - If two sides are congruent, the triangle is _____.
 - If all three sides are congruent, the triangle is _____.
- Use the slope formula to determine if any sides are perpendicular to determine if the triangle is a right triangle.
 - IF** the triangle **IS** a right triangle, the right angle will always be opposite the longest side, so...

Example: Classify $\triangle RST$ by its side lengths. Then determine if the triangle is a right triangle.

Step 1: Use distance formula to find the side lengths:



The triangle has _____ sides, so it is _____.

Step 2: Use slopes to determine if there is a right angle. The two shortest sides are ____ and ____ so find their slopes.

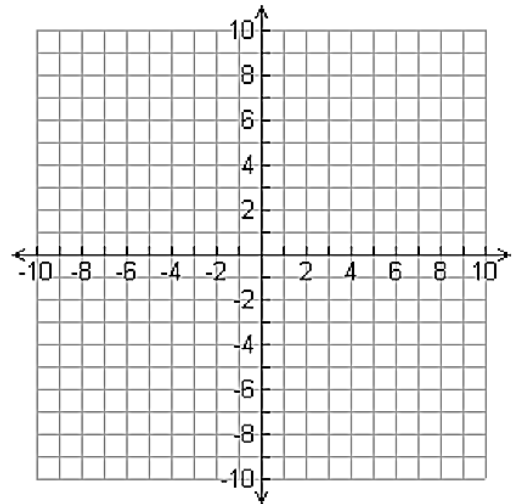
_____ and _____ are/are not perpendicular, therefore \angle _____ is/is not a right angle and $\triangle RST$ is/ is not a _____.

Solution: $\triangle RST$ is _____

Think you got it? Great! Try a couple on your own 😊

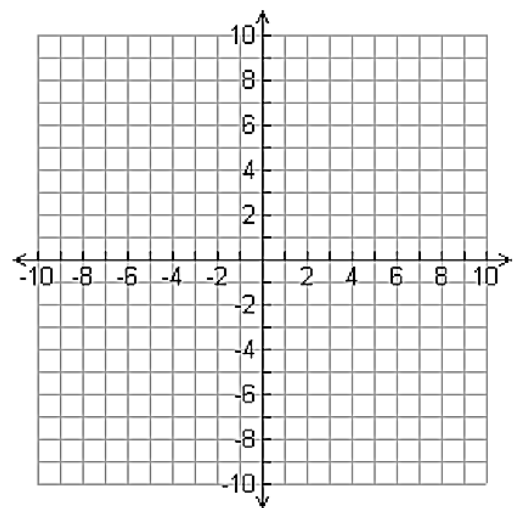
- 1) The vertices of $\triangle XYZ$ are $X(-2,3)$, $Y(-2,-7)$, and $Z(4,-5)$.

Classify $\triangle XYZ$ by its side lengths, then determine if the triangle is a right triangle.



- 2) The vertices of $\triangle PQR$ are $P(-3,-1)$, $Q(-4,4)$, and $R(7,1)$.

Classify $\triangle XYZ$ by its side lengths, then determine if the triangle is a right triangle.



Geometry

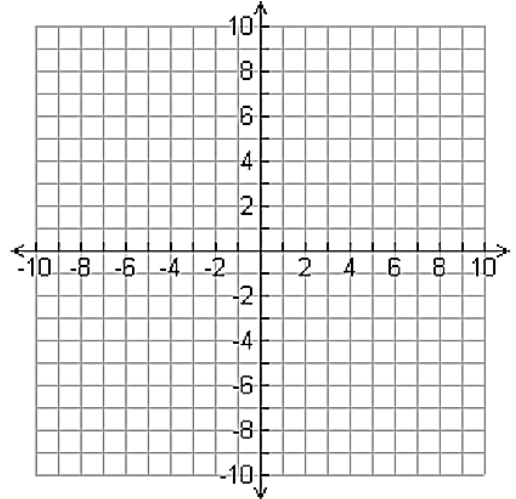
Homework: 4.1/4.7 Coordinate Proofs

Name: _____

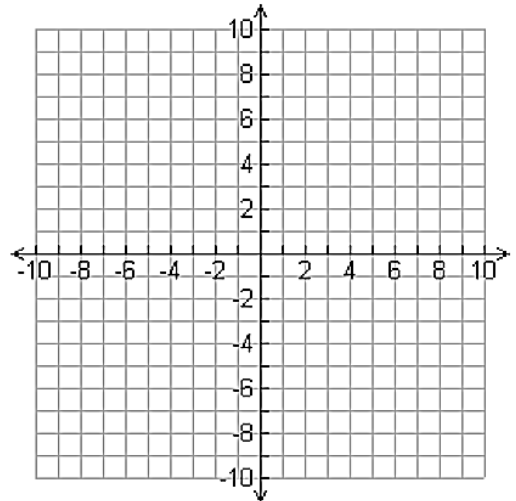
Date: _____ Period: _____

A triangle has the given vertices. Graph the triangle and classify it by its side lengths. Determine if the triangle is a right triangle.

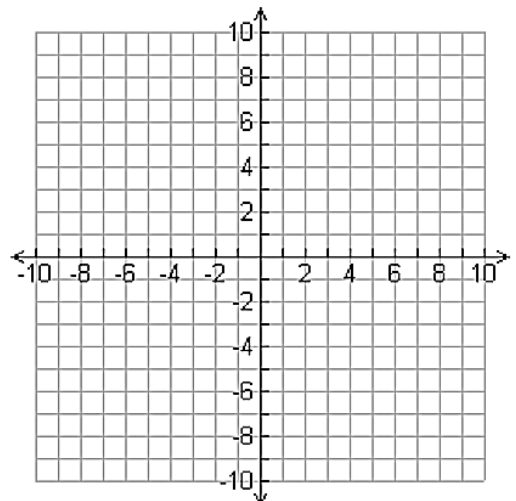
1. $A(-3, 3)$, $B(2, 8)$, $C(7, 3)$



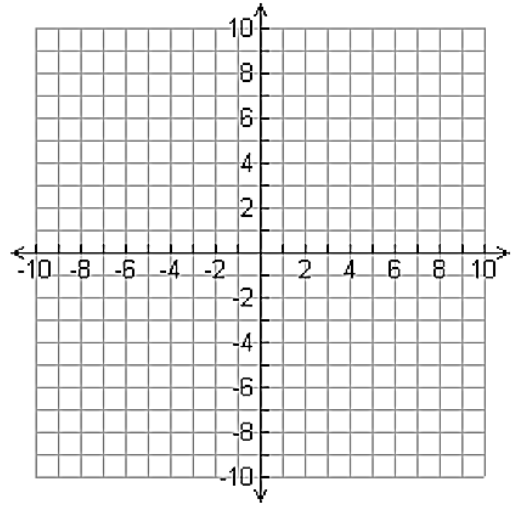
2. $D(1, 1)$, $E(4, 0)$, $F(8, 5)$



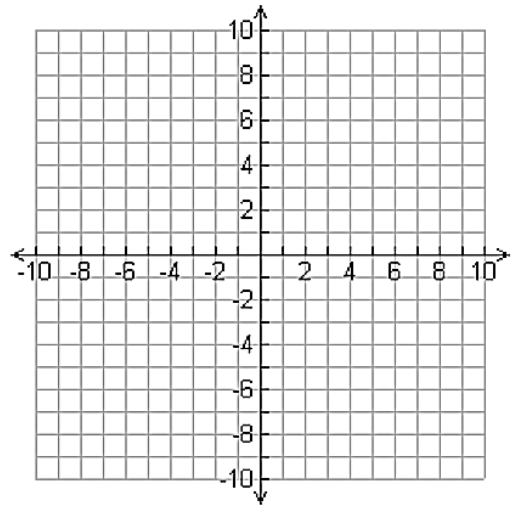
3. $G(1, -3)$, $H(2, -6)$, $I(-1, -5)$



4. $J(0, 0)$, $K(6, 0)$, $L(3, \sqrt{27})$



5. $M(0, 0)$, $N(1, 3)$, $O(3, 1)$



Extension Questions...

6. In $\triangle ABC$, which angles can you conclude are congruent? Why? What is the measure of $\angle A$?
7. Which triangles can you conclude are congruent? Why?
8. In $\triangle JKL$, what is the measure of $\angle K$?

Answers:

1) Right Isosceles 2) Scalene 3) Isosceles 4) Equilateral 5) Isosceles 6) $\angle A \cong \angle B$; both are 45° 7) $\triangle GHI \cong \triangle MNO$ because all of their corresponding sides are congruent. 8) $m\angle K = 60^\circ$